## Bin width

$$
\text { bin width }=\frac{\text { range }}{\# \text { of intervals }}
$$

## Standard Deviation

$$
\sigma=\sqrt{\frac{\sum\left(x_{i}-\bar{x}\right)^{2}}{n}}
$$

IQR

$$
I Q R=Q_{3}-Q_{1}
$$

Z-Score

$$
Z=\frac{x-\bar{x}}{\sigma}
$$

## Weighted Mean

$$
\bar{x}=\frac{\sum x w}{\sum w}
$$

Normal Distribution: $X \sim N\left(\bar{x}, \sigma^{2}\right)$
$\longleftrightarrow \stackrel{99.7 \%}{95 \%} 9$


The graph of the normal distribution $\mathrm{X} \sim \mathrm{N}\left(\overline{\mathrm{x}}, \sigma^{2}\right)$

Additive Principle for the union of two sets

$$
\begin{aligned}
& n(A \cup B)=n(A)+n(B)-n(A \cap B) \\
& P(A \cup B)=P(A)+P(B)-P(A \cap B)
\end{aligned}
$$

## Theoretical Probability

$$
P(A)=\frac{n(A)}{n(S)}
$$

Probability of a Complementary Event

$$
P\left(A^{\prime}\right)=1-P(A)
$$

Conditional Probability

$$
P(B \mid A)=\frac{P(A \cap B)}{P(A)}
$$

Factorial Notation: $n!=n \times(n-1) \times \ldots \times 2 \times 1$

Permutations: $P(n, r)={ }_{n} P_{r}=\frac{n!}{(n-r)!}$
Permutations (with a,b,c like objects) $=\frac{n!}{a!b!c!}$
Combinations: $C(n, r)={ }_{n} C_{r}=\binom{n}{r}=\frac{n!}{(n-r)!r!}$
Expected Value of a Discrete Random Variable

$$
E(X)=\sum x_{i} P\left(X=x_{i}\right)
$$

i.e. multiply each " $x$ " by its probability, then add them

Binomial Probability Distribution

$$
P(X=k)=\binom{n}{k}(p)^{k}(q)^{n-k}
$$

Expected Value of Binomial Distribution $\quad E(X)=n p$ Hypergeometric Probability Distribution

$$
\boldsymbol{P}\left(\boldsymbol{X}=\boldsymbol{x}_{\boldsymbol{i}}\right)=\frac{\binom{a}{x_{i}}\binom{b}{r}}{\binom{n}{r}} \text { or } P\left(X=x_{i}\right)=\frac{\binom{\text { comb. of }}{\text { success }}\binom{\text { comb.of }}{\text { failures }}}{\binom{T O T A L}{\text { COMB }}}
$$

## Z-Score Table $\quad$ example: $P(z \leq 1.15=0.1251)$

|  | 0 | 0.01 | 0.02 | 0.03 | 0.04 | 0.05 | 0.06 | 0.07 | 0.08 | 0.09 |  | 0 | 0.01 | 0.02 | 0.03 | 0.04 | 0.05 | 0.06 | 0.07 | 0.08 | 0.09 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| -2.9 | 0.0019 | 0.0018 | 0.0018 | 0.0017 | 0.0016 | 0.0016 | 0.0015 | 0.0015 | 0.0014 | 0.0014 | 0.0 | 0.5000 | 0.5040 | 0.5080 | 0.5120 | 0.5160 | 0.5199 | 0.5239 | 0.5279 | 0.5319 | 0.5359 |
| -2.8 | 0.0026 | 0.0025 | 0.0024 | 0.0023 | 0.0023 | 0.0022 | 0.0021 | 0.0021 | 0.0020 | 0.0019 | 0.1 | 0.5398 | 0.5438 | 0.5478 | 0.5517 | 0.5557 | 0.5596 | 0.5636 | 0.5675 | 0.5714 | 0.5753 |
| -2.7 | 0.0035 | 0.0034 | 0.0033 | 0.0032 | 0.0031 | 0.0030 | 0.0029 | 0.0028 | 0.0027 | 0.0026 | 0.2 | 0.5793 | 0.5832 | 0.5871 | 0.5910 | 0.5948 | 0.5987 | 0.6026 | 0.6064 | 0.6103 | 0.6141 |
| -2.6 | 0.0047 | 0.0045 | 0.0044 | 0.0043 | 0.0041 | 0.0040 | 0.0039 | 0.0038 | 0.0037 | 0.0036 | 0.3 | 0.6179 | 0.6217 | 0.6255 | 0.6293 | 0.6331 | 0.6368 | 0.6406 | 0.6443 | 0.6480 | 0.6517 |
| -2.5 | 0.0062 | 0.0060 | 0.0059 | 0.0057 | 0.0055 | 0.0054 | 0.0052 | 0.0051 | 0.0049 | 0.0048 | 0.4 | 0.6554 | 0.6591 | 0.6628 | 0.6664 | 0.6700 | 0.6736 | 0.6772 | 0.6808 | 0.6844 | 0.6879 |
| -2.4 | 0.0082 | 0.0080 | 0.0078 | 0.0075 | 0.0073 | 0.0071 | 0.0069 | 0.0068 | 0.0066 | 0.0064 | 0.5 | 0.6915 | 0.6950 | 0.6985 | 0.7019 | 0.7054 | 0.7088 | 0.7123 | 0.7157 | 0.7190 | 0.7224 |
| -2.3 | 0.0107 | 0.0104 | 0.0102 | 0.0099 | 0.0096 | 0.0094 | 0.009 | 0.0089 | 0.0087 | 0.0084 | 0.6 | 0.7257 | 0.7291 | 0.7324 | 0.7357 | 0.7389 | 0.7422 | 0.7454 | 0.7486 | 0.7517 | 0.7549 |
| -2.2 | 0.0139 | 0.0136 | 0.0132 | 0.0129 | 0.0125 | 0.0122 | 0.0119 | 0.0116 | 0.0113 | 0.0110 | 0.7 | 0.7580 | 0.7611 | 0.7642 | 0.7673 | 0.7704 | 0.7734 | 0.7764 | 0.7794 | 0.7823 | 0.7852 |
| -2 | 0.0179 | 0.0174 | 0.0170 | 0.016 | 0.0162 | 0.0158 | 0.015 | 0.0150 | 0.0146 | 0.014 | 0.8 | 0.788 | 0.79 | 0.7939 | 0.7967 | 0.7995 | 0.8023 | 0.8051 | 0.8078 | 0.8106 | 0.8133 |
| -2.0 | 0.0228 | 0.0222 | 0.0217 | 0.021 | 0.0207 | 0.0202 | 0.019 | 0.0192 | 0.0188 | 0.018 | 0.9 | 0.8159 | 0.8186 | 0.82 | 0.8238 | 0.8264 | 0.8289 | 0.8315 | 0.8340 | 0.8365 | 0.8389 |
| -1 | 0.0287 | 0.0281 | 0.0274 | 0.026 | 0.0262 | 0.0256 | 0.025 | 0.024 | 0.0239 | 0.023 | 1.0 | 0.8413 | 0.8438 | 0.846 | 0.8485 | 0.8508 | 0.8531 | 0.8554 | 0.8577 | 0.8599 | 0.8621 |
| -1 | 0.0359 | 0.0351 | 0.0344 | 0.0336 | 0.0329 | 0.0322 | 0.031 | 0.030 | 0.030 | 0.029 | 1.1 | 0.864 | 0.8665 | 0.868 | 0.8708 | 0.8729 | 0.8749 | 0.8770 | 0.8790 | 0.8810 | 0.8830 |
| -1.7 | 0.0446 | 0.0436 | 0.0427 | 0.0418 | 0.0409 | 0.0401 | 0.0392 | 0.0384 | 0.0375 | 0.0367 | 1.2 | 0.8849 | 0.8869 | 0.8888 | 0.8907 | 0.8925 | 0.8944 | 0.8962 | 0.8980 | 0.8997 | 0.901 |
| -1.6 | 0.0548 | 0.0537 | 0.0526 | 0.0516 | 0.0505 | 0.0495 | 0.048 | 0.0475 | 0.0465 | 0.0455 | 1. | 0.9032 | 0.9049 | 0.906 | 0.9082 | 0.9099 | 0.9115 | 0.9131 | 0.9147 | 0.9162 | 0.91 |
| -1.5 | 0.0668 | 0.0655 | 0.0643 | 0.0630 | 0.0618 | 0.0606 | 0.059 | 0.0582 | 0.057 | 0.0559 | 1. | 0.919 | 0.9207 | 0.922 | 0.9236 | 0.9251 | 0.9265 | 0.9279 | 0.9292 | 0.9306 | 0.931 |
| -1.4 | 0.0808 | 0.0793 | 0.0778 | 0.0764 | 0.0749 | 0.0735 | 0.072 | 0.0708 | 0.0694 | 0.0681 | 1. | 0.9332 | 0.9345 | 0.935 | 0.9370 | 0.9382 | 0.939 | 0.9406 | 0.9418 | 0.9429 | 0.944 |
| -1.3 | 0.0968 | 0.0951 | 0.0934 | 0.0918 | 0.0901 | 0.0885 | 0.0869 | 0.0853 | 0.0838 | 0.0823 | 1. | 0.9452 | 0.9463 | 0.947 | 0.9484 | 0.9495 | 0.9505 | 0.9515 | 0.9525 | 0.9535 | 0.9545 |
| -1.2 | 0.1151 | 0.1131 | 0.1112 | 0.1093 | 0.1075 | 0.1056 | 0.1038 | 0.1020 | 0.1003 | 0.0985 | 1.7 | 0.9554 | 0.9564 | 0.9573 | 0.9582 | 0.9591 | 0.9599 | 0.9608 | 0.9616 | 0.9625 | 0.9633 |
| -1.1 | 0.1357 | 0.1335 | 0.1314 | 0.1292 | 0.1271 | 0.1251 | 0.1230 | 0.1210 | 0.1190 | 0.1170 | 1.8 | 0.9641 | 0.9649 | 0.9656 | 0.9664 | 0.9671 | 0.9678 | 0.9686 | 0.9693 | 0.9699 | 0.9706 |
| -1.0 | 0.158 | 0.1562 | 0.1539 | 0.1 | 0.1 | 0.1469 | 0.1 | 0.142 | 0.1401 | 0.1379 | 1.9 | 0.9713 | 0.9719 | 0.972 | 0.9732 | 0.9738 | 0.9744 | 0.9750 | 0.9756 | 0.9761 | 0.9767 |
| -0.9 | 0.184 | 0.1814 | 0.1788 | 0.176 | 0.1736 | 0.171 | 0.168 | 0.1660 | 0.1635 | 0.161 | 2.0 | 0.9772 | 0.9778 | 0.9783 | 0.9788 | 0.9793 | 0.9798 | 0.9803 | 0.9808 | 0.9812 | 0.9817 |
| -0.8 | 0.2119 | 0.2090 | 0.2061 | 0.2033 | 0.2005 | 0.1977 | 0.194 | 0.1922 | 0.1894 | 0.1867 | 2.1 | 0.9821 | 0.9826 | 0.9830 | 0.9834 | 0.9838 | 0.9842 | 0.9846 | 0.9850 | 0.9854 | 0.9857 |
| -0.7 | 0.2420 | 0.2389 | 0.2358 | 0.232 | 0.2296 | 0.2266 | 0.223 | 0.2206 | 0.2177 | 0.2148 | 2.2 | 0.9861 | 0.9864 | 0.9868 | 0.9871 | 0.9875 | 0.9878 | 0.9881 | 0.9884 | 0.9887 | 0.9890 |
| -0.6 | 0.2743 | 0.2709 | 0.2676 | 0.2643 | 0.2611 | 0.2578 | 0.2546 | 0.2514 | 0.2483 | 0.2451 | 2.3 | 0.9893 | 0.9896 | 0.9898 | 0.9901 | 0.9904 | 0.9906 | 0.9909 | 0.9911 | 0.9913 | 0.9916 |
| -0.5 | 0.3085 | 0.3050 | 0.3015 | 0.2981 | 0.2946 | 0.2912 | 0.2877 | 0.2843 | 0.2810 | 0.2776 | 2.4 | 0.9918 | 0.9920 | 0.9922 | 0.9925 | 0.9927 | 0.9929 | 0.9931 | 0.9932 | 0.9934 | 0.9936 |
| -0.4 | 0.3446 | 0.3409 | 0.3372 | 0.3336 | 0.3300 | 0.3264 | 0.3228 | 0.3192 | 0.3156 | 0.3121 | 2.5 | 0.9938 | 0.9940 | 0.9941 | 0.9943 | 0.9945 | 0.9946 | 0.9948 | 0.9949 | 0.9951 | 0.9952 |
| -0.3 | 0.3821 | 0.3783 | 0.3745 | 0.3707 | 0.3669 | 0.3632 | 0.3594 | 0.3557 | 0.3520 | 0.3483 | 2.6 | 0.9953 | 0.9955 | 0.9956 | 0.9957 | 0.9959 | 0.9960 | 0.9961 | 0.9962 | 0.9963 | 0.9964 |
| -0.2 | 0.4207 | 0.4168 | 0.4129 | 0.4090 | 0.4052 | 0.4013 | 0.3974 | 0.3936 | 0.3897 | 0.3859 | 2.7 | 0.9965 | 0.9966 | 0.9967 | 0.9968 | 0.9969 | 0.9970 | 0.9971 | 0.9972 | 0.9973 | 0.9974 |
| -0.1 | 0.4602 | 0.4562 | 0.4522 | 0.4483 | 0.4443 | 0.4404 | 0.4364 | 0.4325 | 0.4286 | 0.4247 | 2.8 | 0.9974 | 0.9975 | 0.9976 | 0.9977 | 0.9977 | 0.9978 | 0.9979 | 0.9979 | 0.9980 | 0.9981 |
| -0.0 | 0.5000 | 0.4960 | 0.4920 | 0.4880 | 0.4840 | 0.4801 | 0.4761 | 0.4721 | 0.4681 | 0.4641 | 2.9 | 0.9981 | 0.9982 | 0.9982 | 0.9983 | 0.9984 | 0.9984 | 0.9985 | 0.9985 | 0.9986 | 0.9986 |

